





Journée commune au CT SED et au GT AFSEC

January 30th, 2025 Paris, France

Ensuring timed-opacity in timed systems

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These works are partially supported by the ANR-NRF research program ProMiS (ANR-19-CE25-0015) and the ANR research program BisoUS (ANR-22-CE48-0012).



Motivation

► Real-time systems:

Not only the functional correctness but also the time to answer is important

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Critical Real-time systems:

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- Failures (in correctness or timing) may result in dramatic consequences



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Threats to a system using non-algorithmic weaknesses

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- Cache attacks
- Electromagnetic attacks
- Power attacks
- Acoustic attacks
- Timing attacks
- Temperature attacks
- etc.

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¹http://home.xnet.com/~warinner/pizzacites.html

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pwd	с	h	i	с	k	е	n
attempt	с	h	е	е	s	е	

Execution time:





Execution time: ϵ





Execution time: $\epsilon + \epsilon$





Execution time: $\epsilon + \epsilon + \epsilon$





Execution time: $\epsilon + \epsilon + \epsilon$

Problem: The execution time is proportional to the number of consecutive correct characters from the beginning of attempt



A specification "The program must be secure"









Inputs

Output

Outline





Outline



Outline

- 1. Preliminaries: Timed model checking
- 2. Timed opacity (& execution-timed opacity)

Outline

Preliminaries: (Parametric) Timed model checking

Timed opacity

Solutions

Conclusion & Perspectives

[AD94]

Finite state automaton (sets of locations)



Finite state automaton (sets of locations and actions)



idleadding sugardelivering coffee

[AD94]

Finite state automaton (sets of locations and actions) augmented with a set X of clocks

Real-valued variables evolving linearly at the same rate



idle adding sugar delivering coffee [AD94]

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Real-valued variables evolving linearly at the same rate

Can be compared to integer constants in invariants

Features

Location invariant: property to be verified to stay at a location



[AD94]

Finite state automaton (sets of locations and actions) augmented with a set X of clocks

Real-valued variables evolving linearly at the same rate

Can be compared to integer constants in invariants and guards

Features

Location invariant: property to be verified to stay at a location
Transition guard: property to be verified to enable a transition



Finite state automaton (sets of locations and actions) augmented with a set X of clocks

Real-valued variables evolving linearly at the same rate

Can be compared to integer constants in invariants and guards

Features

- Location invariant: property to be verified to stay at a location
- Transition guard: property to be verified to enable a transition
- Clock reset: some of the clocks can be set to 0 along transitions







Example of concrete run for the coffee machine

Coffee with 2 doses of sugar

 $\begin{array}{c} x = & 0 \\ y = & 0 \end{array}$



Example of concrete run for the coffee machine

Coffee with 2 doses of sugar





Example of concrete run for the coffee machine

Coffee with 2 doses of sugar





Coffee with 2 doses of sugar










The most critical system: The coffee machine



The most critical system: The coffee machine



The most critical system: The coffee machine



Outline

Preliminaries: (Parametric) Timed model checking

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A first attacker model

Attacker capabilities

- Has access to the model (white box)
- Can observe an execution



A first attacker model

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- Has access to the model (white box)
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Attacker goal

- Wants to deduce some private information based on these observations
 - \rightarrow visit of a private location

Attacker Setting



▶ Observed trace: (*a*, 0.7)(*b*, 1.3)

Attacker Setting



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Question: Can they infer if ℓ_{priv} has been visited ?

Attacker Setting



▶ Observed trace: (*a*, 0.7)(*b*, 1.3)

Question: Can they infer if ℓ_{priv} has been visited ?

No: there is

- ▶ a run visiting ℓ_{priv}
- a run not visiting ℓ_{priv} of trace (a, 0.7)(b, 1.3) too.

Opacity in Timed Automata

The TA is opaque iff all traces can be obtained both

- by runs visiting ℓ_{priv}
- and by runs not visiting it.

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OPAQUE

Opacity in Timed Automata

The TA is opaque iff all traces can be obtained both

- by runs visiting ℓ_{priv}
- and by runs not visiting it.



NON OPAQUE

non-opaque trace: (a, 1)(b, 2)(c, 3)

Decision problem

Opacity Decision Problem

Is the given timed automaton opaque?

[[]Cas09] Franck Cassez. "The Dark Side of Timed Opacity". In: ISA (2009). LNCS. Springer, 2009

Opacity Decision Problem

Is the given timed automaton opaque?

Franck Cassez, The Dark Side of Timed Opacity (2009) \longrightarrow Opacity is undecidable for timed automata!

So... is it the end?

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Opacity Decision Problem

Is the given timed automaton opaque?

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So... is it the end? Not yet!

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Our Contributions

change the system:

subclasses of TA for which opacity can be decided

- restriction on the number of actions
- restriction on the number of clocks
- discrete time
- change the problem \rightarrow weaker attackers
 - bounded number of observations
 - limited observation

Outline

Preliminaries: (Parametric) Timed model checking

Timed opacity

Solutions Low dimension

Bounded number of observations Execution-time opacity

Conclusion & Perspectives

Changing the System

Subclass	Opacity
One-action TAs	×
One-clock TAs without silent actions	non-primitive recc.
One-clock TAs with silent actions	×
(>1)-clock TAs	×
Discrete-time TAs	$\sqrt{\text{EXPSPACE-c.}^2}$
Observable ERAs	$\sqrt{PSPACE-c}$.

Verifying opacity of discrete-timed automata, Klein and al., FormaliSE'24 and in *The opacity of timed automata*, An and al., FM 2024

[[]ÉL24] Sarah Dépernet Étienne André and Engel Lefaucheux. "The Bright Side of Timed Opacity". In: ICFEM. 2024

²Fun fact: decidability result also proved this year in

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Solutions Low dimension Bounded number of observations Execution-time opacity

Conclusion & Perspectives

What if the attacker has a limited observation budget?

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What if the attacker has a limited observation budget?

The attacker can only see the first N observations of the run.



Possible traces with N = 2: $(a, \tau_1)(b, \tau_2)$ with $1 \le \tau_1 \le \tau_2 \le 2$

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- OPAQUE with N = 2
- NON OPAQUE with N = 3: (a, 1)(b, 2)(c, 3)

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Result

The problem of opacity with a bounded number of observations is decidable, and moreover we have a **2EXPSPACE** algorithm.

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Outline

Preliminaries: (Parametric) Timed model checking

Timed opacity

Solutions Low dimension Bounded number of observations Execution-time opacity

Conclusion & Perspectives

Formalization

Hypotheses:

[AS19][TOSEM22]

- \blacktriangleright A start location ℓ_0 and an end location ℓ_f
- ► A special private location ℓ_{priv}



[[]TOSEM22] Étienne André, Didier Lime, Dylan Marinho, and Jun Sun. "Guaranteeing Timed Opacity using Parametric Timed Model Checking". In: <u>ACM TOSEM</u> (2022)

Formalization

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Definition (execution-time opacity)

The system is ET-opaque for a duration d if there exist two runs to ℓ_f of duration d

- 1. one visiting ℓ_{priv}
- 2. one <u>not</u> visiting ℓ_{priv}

[[]TOSEM22] Étienne André, Didier Lime, Dylan Marinho, and Jun Sun. "Guaranteeing Timed Opacity using Parametric Timed Model Checking". In: ACM TOSEM (2022)





• There exist (at least) two runs of duration d = 2:



• There exist (at least) two runs of duration d = 2:

visiting ℓ_{priv}

 $\rightarrow \ell_0$



• There exist (at least) two runs of duration d = 2:





• There exist (at least) two runs of duration d = 2:





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• There exist (at least) two runs of duration d = 2:









▶ There exist (at least) two runs of duration d for all durations $d \in [1, 2.5]$

The system is \exists -ET-opaque



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The system is \exists -ET-opaque

 private durations are [1, 2.5] public durations are [0, 3]



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 public durations are [0, 3]
- ▶ private durations ⊆ public durations



• There exist (at least) two runs of duration d for all durations $d \in [1, 2.5]$

The system is ∃-ET-opaque

- private durations are [1, 2.5]
 public durations are [0, 3]
- ▶ private durations ⊆ public durations

The system is weakly ET-opaque



• There exist $(at \ least)$ two runs of duration d for all durations $d \in [1, 2.5]$

The system is ∃-ET-opaque

- private durations are [1, 2.5]
 public durations are [0, 3]
- ▶ private durations ⊆ public durations

The system is weakly ET-opaque

• private durations \neq public durations



• There exist $(at \ least)$ two runs of duration d for all durations $d \in [1, 2.5]$

The system is \exists -ET-opaque

- private durations are [1, 2.5]
 public durations are [0, 3]
- ▶ private durations ⊆ public durations

The system is weakly ET-opaque

• private durations \neq public durations

The system is not fully ET-opaque



ET-opacity notion	Ξ	Weak	Full
p-Emptiness			
p-Synthesis			



ET-opacity notion	Ξ	Weak	Full
p-Emptiness	×(∃v)	×(∃v)	×(∃v)
p-Synthesis			



ET-opacity notion	Э	Weak	Full
p-Emptiness	×(∃v)	×(∃v)	×(∃v)
p-Synthesis	$0 \le p_1 \le 3$		
	$\land p_1 \leq p_2$		



ET-opacity notion	Ξ	Weak	Full
p-Emptiness	×(∃v)	×(∃v)	×(∃v)
p-Synthesis	$0 \le p_1 \le 3$	$0 \leq p_1 \wedge p_2 \leq 3$	
	$\land p_1 \leq p_2$	$\wedge p_1 \leq p_2$	
	P2	P2	
	P1	P1	



ET-opacity notion	Ξ	Weak	Full
p-Emptiness	×(∃v)	×(∃v)	×(∃v)
p-Synthesis	$0 \leq \mathbf{p}_1 \leq 3$	$0 \leq \mathbf{p}_1 \wedge \mathbf{p}_2 \leq 3$	$\mathbf{p_1}=0\wedge\mathbf{p_2}=3$
	$\land p_1 \leq p_2$	$\land p_1 \leq p_2$	
	P2	P2	

Decidability results for ET-opacity

		∃-ET-opaque	weakly ET-	fully ET-
			opaque	opaque
Decision	ТА	\checkmark	\checkmark	\checkmark
n emptiness	L/U-PTA	\checkmark	×	×
<i>p</i> -emptiliess	ΡΤΑ	×	×	×
n synthosis	L/U-PTA	×	×	×
<i>p</i> -synthesis	ΡΤΑ	×	×	×

- L/U-PTA (Lower/Upper-PTA): subclass of PTA where the parameters are partitioned into two sets (either compared to clocks as upperbound, or as lower bound) [Hun+02]
- Proofs are based on the region automaton (for TAs) and by reduction from EF-emptiness (for PTAs). (see formal proofs in [TOSEM22])

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Expiring ET-opacity

How to deal with outdated secrets?
 e.g., cache values, status of the memory, ...



Idea

The secret can expire: beyond a certain duration, knowing the secret is useless to the attacker (e.g., a cache value) [Amm+21]

Expiring ET-opacity

Assumption

Knowing an expired secret is equivalent to not knowing a secret

	Secret runs	Non-secret runs
FT opacity	Runs visiting the private lo-	Runs not visiting the pri-
	cation	vate location
	(= private runs)	(= public runs)
ovniring ET onacity	Private runs with ℓ_{priv} visit	(i) Public runs and
expiring-Lit-opacity	$\leq \Delta$ before the system	(ii) Private runs with ℓ_{priv}
	completion	visit > Δ before the system
		completion

[[]ICECCS23] Étienne André, Engel Lefaucheux, and Dylan Marinho. "Expiring opacity problems in parametric timed automata". In: ICECCS (2023). Springer, 2023

Decidability results for expiring-ET-opacity

		weakly expiring- ET-opaque	fully expiring- ET-opaque
Δ-emptiness Δ-synthesis	TA		√ ?
$(n \perp \Lambda)$ emptiness	L/U-PTA	×	×
$(p + \Delta)$ -emptiliess	PTA	×	×
$(n \perp \Lambda)$ synthesis	L/U-PTA	×	×
$(p + \Delta)$ -synthesis	PTA	×	×

∃-expiring ET-opacity was left as a future work.

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Decidability results for expiring-ET-opacity

		weakly expiring- ET-opaque	fully expiring- ET-opaque
Δ-emptiness Δ-synthesis	ТА		√ ?
$(n \perp \Lambda)$ -emptiness	L/U-PTA	×	×
$(p + \Delta)$ -emptiness	РТА	×	×
$(n \perp \Lambda)$ synthesis	L/U-PTA	×	×
$(p + \Delta)$ -synthesis	РТА	×	×

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Preliminaries: (Parametric) Timed model checking

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Conclusion & Perspectives

Conclusion

Context: vulnerability by timing-attacks

- Goal: avoid leaking information on whether some discrete state has been visited
- Variations of the notion of timed opacity
 - Model: weaker models considered
 - Attacker: limited number of observations & observability of the global execution time

Several problems studied for timed automata

- Ø Mostly undecidable with observations
- Mostly decidable for weaker attackers

Conclusion

Extension of ET-opacity to parametric timed automata

- Quickly undecidable
- © One procedure for one synthesis problem

Other contributions

- Untimed and timed control
- \blacktriangleright \exists and weak timed opacity with observations

Perspectives

Theoretical perspectives

- Existential version of expiring ET-opacity
- Δ-synthesis for full expiring ET-opacity

Algorithmic perspectives

- Synthesis for weak and full ET-opacity
- Synthesis for expiring problems

Automatic translation of programs to PTAs

Our translation required non-trivial creativity

 Translation with Petri nets including cache system

Perspectives

Theoretical perspectives

- Existential version of expiring ET-opacity
- Δ-synthesis for full expiring ET-opacity

Algorithmic perspectives

- Synthesis for weak and full ET-opacity
- Synthesis for expiring problems

Automatic translation of programs to PTAs

► Our translation required non-trivial creativity → Translation with Petri nets including cache system see you in SAC'25!

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ET-opacity synthesis is (very) difficult

Theorem (Undecidability of ∃-ET-opacity *p*-emptiness)

Given \mathcal{P} , the mere existence of a parameter valuation v s.t. $v(\mathcal{P})$ \exists -ET-opacity is undecidable.

Proof idea: reduction from reachability-emptiness for PTAs



Remark: L/U-PTA is a decidable subclass